

MATH 317 Advanced Calculus of one variable

Fall 2017

Instructor:	Dr. Manuela Girotti; office: Weber 223C
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Time:	Mon-Wed-Fri 9:00am-9:50am
Location:	Engineering E105
Office hours:	Monday $4:00 \text{pm} - 5:30 \text{pm}$ and Thursday $11:00 \text{am} - \text{noon}$
	Weber 008 (basement)
Textbook:	Basic Analysis: Introduction to Real Analysis, Volume I, by Jiří Lebl
	Paperback: 260 pages; 4th edition (March 1, 2016)
	Publisher: CreateSpace Independent Publishing Platform;
	ISBN-10: 1530256747; ISBN-13: 978-1530256747
	downloadable online for free at: http://www.jirka.org/ra/
Catalog	convergence of sequences, series: limits, continuity, differentiation, integra-
description:	tion of one-variable functions; development of skills for proving theorems.
Overview:	This is a proofs-based course, mostly aimed at Mathematics-major students.
	Prerequisite for this course are the two Calculus courses MATH 160 and
	161 which provide already the basic concepts and results of Real Analysis.
	However, the purpose of the present course is to give a deeper and more
	theoretical understanding of the theorems already showed in the previous
	courses and develop them further.



Homework:	you will be required to hand in 5 assignments along the semester. The
	assignments will be posted on the Canvas website (with due dates – please,
	check the Canvas calendar often) and they reflect the content of the course.
	No late assignments will be accepted.

Please, submit your assignment with all the papers stapled together and with your name and CSU ID written on the first page. Use a pen and write clearly.

If you are unable to submit a hard copy assignment, you can also scan it and send it to the instructor by email, no later than the due date and due time.

Discussions and work group are encouraged, however the final submission has to be personal and show understanding of the material. Grades will be posted on Canvas.

- Midtermthere will be 2 midterm tests on Friday September 29th, 2017 andexams:Friday November 10th, 2017. The first one will cover chapters 0-1-2from the book and the second one will cover the subsequent chapters 3 and4. They will be held in class and they will last 50 minutes.
- **Final exam:** the final examination will cover material from the entire course, but emphasis will be given on recent material on integration and open/closed sets as foundations for topology (chapters 5, 6 and 7). It will be a closed-book exam, no notes are allowed.

The final exam is scheduled for Monday December 11th, 2017 between 7:30am and 9:30am. It will be held in class (room E105).

If you have time conflicts with other examinations, please notify the instructor as soon as possible.



Department of Mathematics College of Natural Sciences

Grading	your final grade will be built up from the grades coming from assignments,
scheme:	midterm and final exams in the following percentage:
	20% assignments,
	20% + 20% midterm exams,
	40% final exam.
	Please, note that the grading algorithm on Canvas is set automatically and
	does not respect the above scheme.
Calculators:	unless otherwise stated, basic 4-function calculators and scientific calculators
	(like Sharp EL 531 and Casio FX 300MS, for example) are permitted in class
	tests and final examination.
Academic	as in any other course you will attend, you are required to study and act
Integrity:	according to the University Policy on Academic Integrity and the Student
	Conduct Code (see http://tilt.colostate.edu/integrity).
	Moreover, bear in mind that the consequences for such misconduct (cheating,
	plagiarism, etc.) will ultimately fall upon you: this course is a precious
	opportunity for you to learn something new and valuable. It's an investment
	on your future. Failing to acquire it will sadly be your loss.

<u>IMPORTANT</u>: note that there is no "100% final exam" option in this course. The term work will substantially contribute to the final grade. Therefore, active participation in classes and continuous work on the course material during the semester is essential for success in this course.



Tentative (and ambitious) outline of the course

A diary of the lectures will be regularly kept on the Canvas calendar with the sections covered in each class.

Week	Chapter	Topic	Suggested exercises
$ \begin{array}{c} 1 \\ 08/21 - \\ 08/25 \end{array} $	Ch. 0, 1	Basic Set Theory Basic properties; the set of real numbers	Ch. 0: 3.7, 3.9, 3.10, 3.11, 3.15, 3.20 Ch. 1: 1.2, 1.6, 1.8, 1.9, 1.10; 2.5, 2.6, 2.7, 2.8, 2.11, 2.13
$egin{array}{c} 2 \ 08/28- \ 09/01 \end{array}$	Ch. 1	The set of real numbers; absolute value; intervals and the size of \mathbb{R} ; decimal representation of the real	Ch. 1: 3.2, 3.5, 3.7; 4.4, 4.6, 4.9
$egin{array}{c} 3 \ 09/06- \ 09/08 \end{array}$	Ch. 2	Sequences and limits	Ch. 2: 1.7, 1.8, 1.9, 1.13, 1.15, 1.17, 1.20
$\begin{array}{c} 4 \\ 09/11- \\ 09/15 \end{array}$	Ch. 2	Facts about limits of sequences; limit superior, limit inferior and Bolzano-Weierstrass; Cauchy sequences	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$
5 09/18– 09/22	Ch. 2	Series; more on series	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$
$egin{array}{c} 6 \ 09/25- \ 09/29 \end{array}$	Ch. 3	Limits of functions	Ch. 3: 1.7, 1.9, 1.10, 1.13
$7 \\ 10/02 - \\ 10/06$	Ch. 3	Continuous functions	Ch. 3: 2.3, 2.10, 2.11, 2.14, 2.15, 2.16



8 10/09– 10/13	Ch. 3	Min-max and intermediate value theorem; uniform continuity; limits at infinity; monotone functions and continuity Midterm exam # 1	Ch. 3: 3.3, 3.4, 3.6, 3.8, 3.103.11; 4.3, 4.5, 4.6, 4.9, 4.10, 4.14; 5.7; 6.7, 6.8, 6.11
$9 \\ 10/16 - \\ 10/20$	Ch. 4	The derivative; mean value theorem; Taylor's theorem; inverse function theorem	Ch. 4: 1.1, 1.3, 1.5, 1.8, 1.9, 1.10, 1.12; 2.4, 2.5, 2.7, 2.9, 2.10, 2.11; 3.3, 3.4, 3.6; 4.7, 4.8
$ \begin{array}{c} 10 \\ 10/23 - \\ 10/27 \end{array} $	Ch. 5	The Riemann integral; properties of the integral	Ch. 5: 1.3, 1.7, 1.9, 1.10, 1.11; 2.4, 2.5, 2.6, 2.7, 2.10, 2.11, 2.12, 2.13
11 10/30- 11/03	Ch. 5	Properties of the integral; Fundamental theorem of Calculus	Ch. 5: 3.4, 3.5, 3.7, 3.9, 3.11
12 11/06- 11/10	Ch. 5	The logarithm and exponential; improper integrals	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
$ \begin{bmatrix} 13 \\ 11/13 - \\ 11/17 \end{bmatrix} $	Ch. 6	Pointwise and uniform convergence; interchange of limits Midterm exam # 2	Ch. 6: 1.2, 1.7, 1.9, 1.10; 2.1, 2.2, 2.7, 2.10, 2.11
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$14 \\ 11/27 - \\ 12/01$	Ch. 7	Metric spaces; open and closed sets; sequences and conver- gence; completeness and compactness; continuous functions	Ch. 7: 1.4, 1.7, 1.8; 2.4, 2.5, 2.7, 2.9, 2.10, 2.11; 3.5, 3.6, 3.9, 3.11; 4.2, 4.3, 4.7, 4.8; 5.3, 5.8, 5.9
$egin{array}{c} 15 \ 12/04- \ 12/08 \end{array}$		Review & conclusions	

Disclaimer: the instructor reserves the right to make changes to the course outline and course content should this be necessary for academic or other reasons. Changes will also be posted on Canvas and promptly communicated. Every effort will be made to minimize such changes.